# Equilibrium-line altitudes during the Last Glacial Maximum across the Brooks Range, Alaska 

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#### Abstract

Equilibrium-line altitudes (ELAs) were estimated for 383 reconstructed glaciers across the Brooks Range, northern Alaska, to investigate their regional pattern during the Last Glacial Maximum (LGM). Glacier outlines were delimited based on published field mapping and the original interpretations of aerial photographs. Glacier margins were digitised from 1:63 360-scale maps into a geographic information system (GIS) with a digital elevation model on a $60-\mathrm{m}$ grid. ELAs were calculated for each reconstructed glacier using the accumulation area ratio method ( $A A R=0.58$ ). The analysis was restricted to relatively simple cirque and valley glaciers that deposited clearly identifiable LGM moraines, and that did not merge with the complex transection glacier ice that filled most troughs of the range. The glaciers used in this analysis had areas ranging from 0.14 to $120 \mathrm{~km}^{2}$. Their ELAs rose from 470 m a.s.l. in the western Brooks Range to 1860 m a.s.l. in the east, over a distance of 1000 km . The ELAs were fitted with a third-order polynomial trend surface to model their distribution across the range, and to investigate the source of local-scale variations. The trend surface lowers toward the west and south, similar to previously derived trends based on glaciation thresholds. In addition, ELAs in the northeastern part of the range lower northward toward the Beaufort Sea, which has not been reported as strongly in other studies. Modern glacier ELAs also lower toward the southwest. The depression of LGM ELAs from modern glacier ELAs is greatest in the central Brooks Range (a maximum of 700 m ), and decreases to the east ( 200 m ). The regional pattern of LGM ELAs points to the primary source of moisture from the North Pacific, as it is today. The unexpected trend of LGM ELAs in the northeast part of the range is supported by recent field mapping, where anomalous ice distribution and ELAs reflect complicated LGM climate patterns and possibly late Quaternary tectonism. Copyright © 2005 John Wiley \& Sons, Ltd.


KEYWORDS: equilibrium-line altitude; Brooks Range; Last Glacial Maximum; Alaska.

## Introduction

The equilibrium-line altitude (ELA) of mid- and high-latitude alpine glaciers is controlled mainly by summer temperatures and winter precipitation. Reconstructing the ELA of palaeoglaciers on the basis of geomorphic evidence provides a quantitative means of interpreting past climate during former intervals of presumed steady-state conditions. The regional trend of reconstructed ELAs can be examined to infer past atmospheric circulation and temperature patterns, because the ELA gradient lowers toward accumulation-season moisture or cold ablationseason temperatures. Differences between the ELAs of extant glaciers and those reconstructed from Pleistocene moraines reflect differences between present and full-glacial atmospheric conditions. The geometry of the ELA trend surface

[^0]can itself be used to investigate the controls on ELAs. Although summer temperature and winter precipitation are most important, factors such as aspect, slope, shading, size, shape, and local geography of a glacier may cause an ELA to be above or below the regional trend. Relationships between the magnitude of the deviation of glaciers from the regional trend and the physiographic characteristics of glaciers can be used to identify the factors that lead to local-scale perturbation of the ELA surface.
This study provides a detailed analysis of ELAs across the Brooks Range of northern Alaska. We focus on the maximum position of valley and cirque glaciers during the local Last Glacial Maximum (LGM), for which the morainal evidence is most clear for delimiting past glacier extent. A total of 383 reconstructed glaciers were digitised and analysed in two geographic information systems (GIS) to estimate their former ELAs. A trend surface was fitted to these data to model their spatial variation across the Brooks Range and to interpret the regional controls on ELAs in northern Alaska during the LGM. This record of ELAs for the Brooks Range refines the earlier work of

Porter et al. (1983), whose analysis of glaciation thresholds provided a general illustration of climate patterns across northern Alaska during the LGM.

## Setting

Except for the Cordilleran Ice Sheet in the south, Alaska during the LGM was largely unglaciated due to its isolation from major sources of moisture (Hamilton, 1994; Kaufman and Manley, 2004). Sea-ice cover reduced the moisture available from the north and west, and the exposure of the Bering/Chukchi Platform increased the continentality across central Alaska. Glaciation during the LGM in most of Alaska was therefore restricted to alpine areas. Ice was more extensive during the early part of the late Pleistocene when sea level was higher and global ice volume relatively low (e.g. Kaufman et al., 2001).

The Brooks Range is ca. 1000 km long extending from west to east across northern Alaska. The range is highest in the east reaching over ca. 2700 m a.s.l. in elevation (Fig. 1). The northsouth width of the range varies from ca. 180 to 200 km , with a total area of about $190000 \mathrm{~km}^{2}$. The western Brooks Range, ca. 90 km inland of the Chukchi Sea, consists of the De Long and Baird Mountains, while the central and eastern parts of the range form a single chain of mountains that trends west-east in the central Brooks Range and trends northeast toward the Beaufort Sea in the eastern Brooks Range.

The broad expanse and topographic diversity of the Brooks Range gives rise to a variety of climatic regimes. Because only a few weather stations are scattered around northern Alaska, descriptions of the climate of the Brooks Range are mainly characterised by regional summaries (Fahl, 1975; Péwé, 1975; Daly et al., 1994; Mock et al., 1998), and short-term climate investigations (Haugen, 1979; Wendler et al., 1974, 1975). In the eastern and central parts of the range, the domi-
nant temperature and precipitation gradients are from north to south (Manley and Daley, 2005). South of the divide, the climate is continental, with large temperature extremes, mean annual air temperatures (MAT) from -4 to $-8^{\circ} \mathrm{C}$, and discontinuous permafrost. North of the divide, the climate is arctic, with MAT from -8 to $-12{ }^{\circ} \mathrm{C}$, and continuous permafrost (Péwé, 1975). Temperatures decrease north of the range toward the Beaufort and Chukchi Seas (Haugen, 1979; Daly et al., 1994). The western Brooks Range is more maritime, with temperatures from -7 to $-9^{\circ} \mathrm{C}$. Mean annual precipitation generally decreases to the north and east across the range, from ca. 30 cm in the west to ca. 15 cm in the northeast, although gauges on McCall Glacier in the northeast (Wendler et al., 1974, 1975) recorded mean annual precipitation of ca. 50 cm , between 1969 and 1972, much higher than in other parts of the range.

Modern glaciers are most numerous in the central Brooks Range, where they occupy the highest north-facing cirques. The eastern Brooks Range has the largest glaciers, which are up to 10 km in length around Mount Chamberlin and Mount Michelson (Fig. 1), where the range reaches its peak elevations. The elevation of modern glaciation thresholds increases from 1700 m a.s.l. in the west to 2300 m a.s.l. in the east, but decreases to 2000 m a.s.l. in the northeast (Porter et al., 1983). The trend of modern glacier thresholds is similar to the trend of precipitation, which indicates that presently, moisture availability strongly influences the distribution of glaciers across the Brooks Range.

Pleistocene glaciers covered most of the central and eastern Brooks Range, and parts of the De Long and Baird Mountains in the west (Fig. 1). Glaciers formed at lower elevations in the western Brooks Range, and large transection glaciers (interconnected systems of large, low-lying valley glaciers with poorly defined ice divides) occupied most of the major river valleys in the central and eastern Brooks Range. Late Wisconsin glaciation thresholds in the western Brooks Range decreased in elevation toward the southwest to 900 m a.s.l., and rose to


Figure 1 Shaded relief map of northern Alaska showing the extent of glacier ice (in red) during the Last Glacial Maximum across the Brooks Range (Kaufman and Manley, 2004) and the bathymetry (m) of the continental shelves of the Chukchi and Beaufort Seas. Black solid line indicates the extent of surficial geologic mapping by Hamilton (1978a, 1978b, 1979a, 1979b, 1980, 1981, 1984a, 1984b, 2002a, 2002b, 2003)

2100 m a.s.I. in the eastern Brooks Range, where the gradient of the trend shifted to a more southerly orientation (Porter et al., 1983).

The Pleistocene glacial geology of the Brooks Range is reviewed by Hamilton (1986, 1994). We rely on his subdivision of glaciations and age control in this study. In the Brooks Range, Late Pleistocene glacier advances are nominally assigned to the Itkillik glaciation, and are divided into the Itkillik I glaciation (early Wisconsin sensu lato), and the Itkillik II glaciation, which constitutes the local LGM and is coeval with the late Wisconsin. During the Itkillik II glaciation, glaciers were less extensive than during the Itkillik I glaciation. Itkillik II ice reached only 25 km north of the Brooks Range, compared to Itkillik I ice that extended 40 km north of the range. The age of the Itkillik II glaciation is bracketed between 24 and 15 ka . Itkillik II drift is characterised by topographically irregular deposits that are steeper, more bouldery, and less vegetated than drift of Itkillik I age. Moraines have multiple crests and other primary constructional features and greater relief than moraines of Itkillik I age. A readvance of Itkillik II ice occurred between 13 and 11.5 ka (Hamilton, 2003). This advance left distinctive moraines that are morphologically similar to deposits of the Itkillik II glacial maximum. Glaciers extended up to $15-20 \mathrm{~km}$ north of the range front in some valleys and less extensive moraines in other valleys.

## Methods

Our investigation of ELAs proceeded in four steps. (1) The extent of Itkillik II glaciers were reconstructed on the basis of glacial geomorphic evidence interpreted from aerial photographs and observed in the field. (2) Palaeoglacier outlines were digitised into a GIS to calculate and display spatial variations of glacier physical attributes. (3) A three-dimensional trend surface was created to express the variability of ELAs across the Brooks Range. And (4) the residual values (the deviation of palaeoglacier ELAs from the trend surface) were compared with glacier attributes to infer local factors influencing ELAs.

## Identifying and reconstructing LGM glaciers

Ninety per cent of the 383 palaeoglaciers were reconstructed by interpretation of aerial photographs, and about $10 \%$ were checked by field observations. All were cirque and valley glaciers situated above or beyond, but not confluent with, the larger transection ice that filled the valleys within most of the Brooks Range. These smaller palaeoglaciers provide simpler systems for which the division between the accumulation and ablation area is more easily defined, therefore allowing the ELA to be derived more confidently. The 383 palaeoglaciers include nearly all of the LGM valley and cirque glaciers that could be located. Gaps in the spatial distribution of the glaciers across the range reflect the absence of cirque and valley glaciers during the LGM.

The accuracy of the ELA analysis depends on the ability to identify confidently LGM glacial landforms, and on the consistency of techniques used to map palaeoglacier outlines. The location of LGM moraines used to reconstruct the former glaciers began with Hamilton's 1:250 000-scale surficial-geologic maps, which cover most of the central Brooks Range (Fig. 1) (Hamilton, 1978a, 1978b, 1979a, 1979b, 1980, 1981,

1984a, 1984b, 2002a, 2002b, 2003). LGM glaciers in the western and eastern Brooks Range, not covered by Hamilton's mapping, were mapped for this study from aerial photographs and field observations (Balascio, 2003; Balascio et al., in press). All reconstructed palaeoglacier outlines were then plotted onto 1:63 360-scale topographic maps.
Glacial erosional and depositional features ascribed to the Itkillik II glaciation are typically well expressed in aerial photographs. Cirques last occupied by Itkillik II glaciers are backed by fresh, steep headwalls, and relatively level cirque floors, and moraines exhibit sharp crests and hummocks. The outlines of palaeoglaciers were reconstructed using these cirque and moraine morphologies as well as trimlines, when visible, to infer ice thickness. Consistency among palaeoglacier reconstructions was maintained by assuming uniform up-glacier ice thickness, and that cirques were completely filled with ice by drawing the upper limit generally following the highest most continuous contour of the cirque headwall. Although some subjectivity is involved from cirque-to-cirque, the accuracy of this measurement has little effect on the area of the glacier because of the steepness of cirque headwalls. Because moraines of late Itkillik II and maximum Itkillik II are morphologically similar, the two might have been confused in some valleys, which would result in erroneously high ELAs. However, Hamilton distinguishes between late Itkillik II and LGM moraines in most areas, and our interpretations generally follow his extensive field-based work.
The spatial density of the 383 palaeoglaciers used in this study is somewhat less than has been used in previous studies. For the Brooks Range, the density is approximately two palaeoglaciers per $1000 \mathrm{~km}^{2}$ in an area of ca. $190000 \mathrm{~km}^{2}$, with 47 palaeoglaciers in the eastern, 228 paleoglaciers in the central, and 108 palaeoglaciers in the western Brooks Range. Similar studies in other mountain ranges were based on slightly higher concentrations of data points (glacier ELAs or glaciation threshold elevations). For example, Hawkins' (1985) study of the Merchants Bay area, Baffin Island, was based on 14 points per $1000 \mathrm{~km}^{2}$ in an area of $2500 \mathrm{~km}^{2}$, Leonard's (1984) study of the San Juan Mountains, Colorado, was based on four points per $1000 \mathrm{~km}^{2}$ in an area of $22500 \mathrm{~km}^{2}$ area, and Locke's (1990) study of western Montana was based on three points per $1000 \mathrm{~km}^{2}$ in an area of $176000 \mathrm{~km}^{2}$.

## GIS analysis

The GIS made it possible to easily calculate a variety of physical characteristics for many glaciers and provided a means of clearly illustrating spatial data across a broad area. Two software packages were used: ArcGIS and MFWorks. GIS procedures were developed to calculate former ELAs and glacier attributes from mapped glacier outlines using 60-m grid digital elevation models (DEMs), ArcGIS commands, and the MFWorks scripting language. The surfaces of the former glaciers were interpolated from the digitised glacier outlines and used to calculate the ELA, area, slope, aspect, perimeter, and volume for each palaeoglacier. Compactness was also calculated $\left(4 \pi A / P^{2}\right.$, where $A=$ area and $P=$ perimeter), and is a non-dimensional measure of circularity ranging from 0.0 for a straight line to 1.0 for a circle (Allen, 1998). Similar geospatial analyses of glaciers are presented in Manley (in press).
Errors are associated with the transfer of palaeoglacier outlines to digital format and the interpolation of palaeoglacier surface elevations used to derive the ELA. Errors with the use of GIS stem from the DEMs, which are the basis for calculating the physical characteristics of glaciers. The United States

Geological Survey standards for the DEMs used in this study have root-mean-squared (RMS) errors of less than one-half of the contour interval (RMS ca. 10-15 m). Greater uncertainty is probably associated with the subjectivity of reconstructing glacier outlines, which was minimised by applying consistent techniques to outlining former glaciers.

The variety of methods used to reconstruct former ELAs was recently summarised by Benn et al. (2005). In this study, palaeo-ELAs were estimated on the basis of the accumulation area ratio method (AAR), which has been shown to produce consistent results (Porter, 2001). This method assumes a fixed ratio between the accumulation and ablation areas of a glacier. Different ratios have been applied, ranging from 0.5 to 0.8 , although most use $0.60-0.65$. We used a recently derived ratio of 0.58 , which is based on a global analysis of average AARs for steady-state mass balance of modern glaciers (Dyurgerov, pers. comm.; see Dyurgerov, 2002). To determine how much the choice of an AAR affects the estimated ELA, we applied a range of AAR values in a sensitivity analysis. The results from the Brooks Range glaciers analysed in this study show that, by changing the inferred AAR by $\pm 0.1$, the average ELA changes by only $\pm 35 \mathrm{~m}$ (Balascio, 2003), which is small compared to the overall ELA gradient, and the LGM ELA depression. Similarly, if the inferred AAR varied with climate across the region, we argue that the influence would be secondary to the overall trend of ELAs, and to more important local factors involving debris cover and topographic shielding. Regardless of the accuracy of the ELA value, the choice of an AAR does not impact the first-order spatial trends that are the focus of this study.

The map of ELAs was then used to create three-dimensional surfaces to represent the ELA distribution across the Brooks Range. In the GIS, each glacier was represented by its ELA at a single point. These single points, or 'centroids', were located by GIS scripting at the approximate midpoint of the glacier's long and short axes. ELAs were then contoured and fit with first through fourth order polynomials to examine the good-ness-of-fit of progressively higher-order polynomials. Residual values were calculated for each glacier to statistically compare
the trend surfaces. The residual values were regressed against each glacier characteristic to identify significant relationships.

## Results and discussion

## Palaeo-ELAs

The distribution of the 383 reconstructed glaciers is not uniform across the range (Fig. 2). LGM cirque and valley glaciers in the Brooks Range were clustered on the edge of the range, especially in the south where snowline intersected the landscape, but where ice did not smother the mountains as it did near the crest of the range. In addition, there is a gap in former cirque and valley glaciers between the central and northeastern Brooks Range in the Philip Smith Mountains. The north-tosouth distribution of data points is also limited in the east, where the mountains held extensive transection glaciers.

Reconstructed LGM cirque and valley glaciers vary in size, shape, and elevation (Table 1), with areas ranging from 0.14 to $120 \mathrm{~km}^{2}$, compactness from 0.03 to 0.71 , slope from $4^{\circ}$ to $30^{\circ}$, and volume from 0.002 to $17 \mathrm{~km}^{3}$. Glacier aspects range in all directions, although $93 \%$ are north-facing between $280^{\circ}$ and $80^{\circ}$, with only 26 glaciers facing more southerly. The locations and physical characteristics of all of the glaciers reconstructed in this study are listed in the Appendix.

Palaeo-ELAs rise from west to east across the Brooks Range (Fig. 2). The rise appears to occur in two major steps, one with a slope of $3.8 \mathrm{~m} \mathrm{~km}^{-1}$ at ca. $155^{\circ} \mathrm{W}$ longitude, and the other with a slope of $3.3 \mathrm{~m} \mathrm{~km}^{-1}$ at $144^{\circ} \mathrm{W}$. Alternatively, the lack of ELA change in the area separating these steps might result from the sparse data coverage in this zone. LGM ELAs increase from 470 m a.s.l. in the De Long Mountains to 1860 m a.s.l. in the Romanzof Mountains. Generally, ELAs tend to be higher over the highest massifs and lower over the Noatak Basin and along the southern range front. The palaeo-ELAs decrease in


Figure 2 Contoured equilibrium-line altitudes for 383 Last Glacial Maximum valley glaciers across the Brooks Range. Black dots show the location of reconstructed glaciers. Contours were generated using a geographic information system interpolation method (Balascio, 2003). Contour interval is 100 m

Table 1 Summary of physical characteristics of reconstructed Last Glacial Maximum valley glacier $(n=383)$

|  | Minimum | Maximum | Median | Average $\pm 1 \sigma$ |
| :--- | :---: | :---: | :---: | :---: |
| Slope $\left({ }^{\circ}\right)$ | 4 | 30 | 11 | $12 \pm 4.4$ |
| Area $\left(\mathrm{km}^{2}\right)$ | 0.14 | 120 | 0.84 | $2.3 \pm 6.9$ |
| Volume $\left(\mathrm{km}^{3}\right)$ | 0.002 | 17 | 0.05 | $0.19 \pm 0.89$ |
| Compactness ${ }^{\mathrm{a}}$ | 0.03 | 0.71 | 0.43 | $0.41 \pm 0.14$ |
| Length $(\mathrm{km})$ | 0.40 | 12.7 | 1.4 | $1.9 \pm 1.5$ |
| ELA $(\mathrm{m})$ | 468 | 1859 | 854 | $963 \pm 325$ |

${ }^{\text {a }}$ Measure of circularity $\left(4 \pi A / P^{2}\right.$, where $A=$ area and $P=$ perimeter).
the northeasternmost part of the range, from 1600 to 1700 m a.s.l. over the Mount Michelson and Mount Chamberlin areas, to 1500 m a.s.l. in the eastern Romanzof Mountains. Locally anomalous palaeo-ELAs result in isolated high contours, especially in the western Brooks Range, whereas analogous areas of isolated low contours are not seen.

## Trend surfaces

Statistically fit trend surfaces were calculated for palaeo-ELAs across the Brooks Range to find the surface that best represents the regional variability of ELAs. Regional-scale changes refer to trends on the order of hundreds of kilometres that reflect the broad pattern of climate that controls ELAs, as opposed to local-scale changes that reflect topographic, or geographic effects at scales of tens of kilometres. Four trend surfaces were calculated (Balascio, 2003). A first-order fit created a planar surface that slopes to the southwest $\left(230^{\circ}\right)$ from 1700 to 600 m a.s.l., at $1.1 \mathrm{~m} \mathrm{~km}^{-1}$. The second-order polynomial created a surface that ranges in elevation from 500 to 1800 m a.s.l., with a broad ridge dividing the southwestern dip of the palaeo-ELA surface in the central and western Brooks Range from the northwestern dip of the palaeo-ELA surface in the eastern Brooks Range. The surface slopes gently (ca. $1.3 \mathrm{mkm}^{-1}$ ) along the north flank of the western and central Brooks Range and steeper (ca. $2.6-4.0 \mathrm{~m} \mathrm{~km}^{-1}$ ) along the southern flank of the range. The trend surface maintains a southwestern dip from west to east along the southern flank of the range. In the northeastern Brooks Range the surface slopes uniformly at ca. $3.3 \mathrm{~m} \mathrm{~km}^{-1}$. The third-order polynomial (Fig. 3) exhibits a sharper ridge that more closely follows the crest of the range. Along the southern flank of the range, this surface forms a trough extending from west to east, more closely following the actual palaeo-ELA values. ELA gradients range from ca. 1.4 to $13 \mathrm{~m} \mathrm{~km}^{-1}$, with the steepest portion of the surface dipping north in the northeastern Brooks Range. In the western Brooks Range the surface faces southward, similar to the second-order fit, but exhibits a progression to a southern dip eastward across the range. In the northwest corner of the range, the surface dips north, but this trend is supported by few data points. A fourthorder surface was created and infers even greater changes between palaeo-ELAs of closely spaced glaciers, with slopes ranging up to $13.5 \mathrm{~m} \mathrm{~km}^{-1}$.

The contoured palaeo-ELA data together with goodness-of-fit statistics were used to determine which modelled surface best represents the regional variability of ELAs across the Brooks Range. Visual comparison of the contoured palaeoELA data shows that the third-order trend surface best coincides with the major (100-km-scale) trends in the ELAs across the Brooks Range. RMS and chi-squared statistics show that increasing polynomial orders yields diminishing benefits (Table 2). At
orders higher than third order, differences in RMS and chisquared values between the surfaces are minor. We therefore elect to represent the regional palaeo-ELA across the Brooks Range using a third-order trend surface.

The contoured trend surface of the LGM ELAs is broadly similar to Porter et al.'s (1983; their Fig. 4-4) contoured LGM glaciation threshold altitudes for the Brooks Range. As expected, the ELAs (600-1800m a.s.l.) are systematically lower than glacial thresholds (900-2100 m a.s.l.), because glaciation thresholds are commonly $100-200 \mathrm{~m}$ above ELAs (Meierding, 1982). Both the glaciation threshold and the ELA surfaces decrease toward the southwest in the western part of the range. In the central Brooks Range, glaciation thresholds dip toward the south whereas the ELA trend surface maintains a southwestern dip across the range. In the northeastern Brooks Range, ELAs decline toward the north and slightly to the east, a trend that is incongruent with the rest of the range and that is not exhibited as strongly from glaciation threshold interpretations. Porter et al. (1983) show a slight lowering to the north, indicated by their single-dashed contour just west of Mount Chamberlin.

The palaeo-ELAs in the northeastern Brooks Range are supported by detailed, on-the-ground, glacial-geologic field mapping (Balascio, 2003; Balascio et al., in press). They are unexpected because ELAs typically rise in the lee side of a mountain range in response to precipitation shadows. The lower ELAs reconstructed for the northeasternmost glaciers probably reflects their proximity to the Beaufort Sea, where summer temperatures are lower in response to a shorter duration of seasonally open water.

## Residual values

Residual values were used to explore relationships between the physical characteristics of the palaeoglaciers and their deviation from the trend surface. Residuals were calculated as the difference between the palaeo-ELA derived from the AARs and the modelled value derived using the coordinates for each glacier centroid and the third-order polynomial. The spatial and frequency distributions were studied to identify the factors that may influence the residual values. The frequency of residual values is evenly distributed above and below the trend surface (Fig. 4). Furthermore, there are no systematic regional trends in residual values, indicating that either our choice of a single AAR value across the range was appropriate or, if not, then at least the residual values are not biased by the assumption of a uniform AAR. The average of the absolute value of the residuals is $91 \pm 77 \mathrm{~m}$, similar to the RMS. Spatially, the highest residuals coincide with the highest massifs (Balascio, 2003). This relation is also expressed by the tendency ( $p<0.01$; Table 3) for residual values to be higher for glaciers at higher elevations. High ELAs in the tallest massifs of a range have also been found by others (Leonard, 1984; Locke, 1990), and interpreted to represent moisture diversion around the highest parts of the ranges.
Palaeoglacier ELAs also deviate from the regional trend as a function of glacier size, perhaps for the same reason. Although most mapped glaciers were small (ca. $60 \%$ with areas less than $1 \mathrm{~km}^{2}$; ca. $70 \%$ with volumes less than $0.1 \mathrm{~km}^{3}$; ca. $65 \%$ with lengths less than 2 km ), the inverse relations of area and volume to residual value, and the positive relations of slope and compactness to residual value demonstrate a significant ( $p<0.01$ ) relationship between glacier size and residual value (Table 3). These four characteristics all relate to the size of a glacier and covary (e.g. area and volume). In most cases, the slope of a


Figure 3 Reconstructed equilibrium-line altitude (ELA) surface for the Last Glacial Maximum across the Brooks Range. (A) Relief map of the Brooks Range showing contours of the third-order trend surface and the location of glaciers used to create the surface (black dots). (B) Topographic profile from $C$ to $C^{\prime}$ across the crest of the Brooks Range showing the ELA surface in relation to local relief and the modern glacier ELA third-order trend surface
glacier is related to the size of a glacier because smaller glaciers (less than ca. $2 \mathrm{~km}^{2}$ ) occupy the heads of valleys within the steep peaks of mountains. Larger glaciers extend farther down-valley and flow onto and erode troughs with lower slopes. Compactness is a measure of a glacier's circularity, and clearly distinguishes between long, linear valley glaciers and more rounded cirque glaciers. Regressions of these characteristics show that smaller LGM glaciers tend to lie above the regional ELA trend surface. This is somewhat unexpected because previous work has shown that small glaciers sheltered in deeply eroded cirques, shaded by steep headwalls typically
persist at lower altitudes than their larger neighbours (Clark et al., 1994). Similarly, the ELA would have been lower for debris-covered glaciers, which might have been more prevalent at higher elevations. The tendency for small glaciers to lie above the ELA trend surface may reflect the drying of air masses at higher elevation. The effect of orographic uplift of air on limiting glacier size may be stronger than the beneficial shading effects of deep cirques. Although this trend may represent a local-scale climate effect, the relation between residual value and glacier size is not strong, as indicated by the low $R^{2}$ values.

Table 2 Summary statistics for equilibrium-line altitude trend-surface fits of four different polynomial orders

| Order $^{\mathrm{a}}$ | $\mathrm{RMS}^{\mathrm{b}}(\mathrm{m})$ | $\chi^{2}$ |
| :--- | :---: | :---: |
| 1st | 157 | $9.39 \mathrm{E}+06$ |
| 2nd | 133 | $6.75 \mathrm{E}+06$ |
| 3rd | 119 | $5.41 \mathrm{E}+06$ |
| 4th | 115 | $5.03 \mathrm{E}+06$ |

${ }^{\mathrm{a}} y=b+x_{1}+x_{2}=T_{1}$
$y=T_{1}+x_{1}{ }^{2}+x_{1} x_{2}+x_{2}{ }^{2}=T_{2}$
$y=T_{2}+x_{1}{ }^{3}+x_{1}{ }^{2} x_{2}+x_{1} x_{2}{ }^{2}+x_{2}{ }^{3}=T_{3}$
$y=T_{3}+x_{1}^{4}+x_{1}^{3} x_{2}+x_{1}^{2} x_{2}^{2}+x_{1} x_{2}^{3}+x_{2}^{4}=T_{4}$
${ }^{\mathrm{b}} \mathrm{RMS}=$ root mean squared.

Aspect also covaries with residual value, although only weakly (Table 3). The relationship between glacier aspect and deviation from the regional ELA trend is expected because glaciers that face toward the north are more shaded from solar radiation than those facing south, and tend to have lower ELAs. Generally, the south-facing glaciers have ELAs that are above the regional trend rather than below it, although there are a few north-facing glaciers with high residual values and a few south-facing glaciers with low residual values.

## Implications for LGM atmospheric circulation across Alaska

The ELAs of modern glaciers in the Brooks Range were examined to compare with the trends from the palaeoglaciers. Modern ELAs were determined using similar methods to those used to estimate LGM ELAs. Modern glacier ELAs were estimated using an AAR of 0.58 applied to 940 glacier outlines taken from USGS 1:63 360-scale topographic maps and with USGS DEMs
derived from the same maps. The modern glacier ELA data were also fit with a third-order polynomial trend surface to represent their regional variation.

The southwest-sloping regional palaeo-ELA trend is similar to the overall trend of the modern glacier ELAs across the Brooks Range (Fig. 3). The similarity indicates that, like today, LGM mountain glaciers in the Brooks Range were strongly influenced by moisture availability, which was supplied dominantly from the southwest. A southwest moisture source is also manifested by modern glacier ELAs that rise on the lee side of the central Brooks Range. In detail, the trend surface of modern glacier ELAs is lowest, and relatively horizontal at ca. 1600 m a.s.I. in the central Brooks Range. Modern ELAs rise to 2100 m a.s.l. as summit elevations increase in the eastern Brooks Range.

The difference between modern and LGM ELAs $(=\Delta$ ELA $)$ was larger in the central Brooks Range (a maximum of ca. 700 m) than in the eastern Brooks Range (ca. 200 m) where glacier elevations are higher (Fig. 3). This minor depression in the eastern Brooks Range may indicate the influence of postglacial tectonic uplift that elevated moraines locally (Porter et al., 1983). The rapidity of uplift would have been remarkable, however, and without significant geomorphic evidence of postglacial tectonic activity. The tendency toward lower $\triangle E L A$ values with increasing glacier elevation has been documented elsewhere (e.g. Mark et al., 2005), and has been attributed to the influence of basin morphometry on the response of glaciers to climatic change. Alternatively, the eastward decrease in $\Delta$ ELA might indicate increased Holocene sea-surface temperatures and reduced sea ice that allow moisture from the Beaufort Sea to nourish glaciers inland and to lower modern glacier ELAs (Balascio et al., in press).
The magnitude of LGM ELA lowering in the Brooks Range is similar to other parts of Alaska where values are typically ca. 300-600 m (Hamilton and Porter, 1975; Kaufman and Hopkins, 1986; Mann and Peteet, 1994; Stillwell and Kaufman, 1996; Manley et al., 1997; Briner and Kaufman, 2000).


Figure 4 Histogram of residuals above and below the third-order reconstructed equilibrium-line altitude trend surface

Table 3 Least-squares regressions of glacier characteristics against residual values from the third-order reconstructed equilibrium-line altitude trend surface

|  | $Y$-intercept | $X$ value | $R^{2}$ | $p$ |
| :--- | :---: | ---: | :---: | :---: |
| Slope $\left({ }^{\circ}\right)$ | 12.0 | $8.18 \mathrm{E}-03$ | 0.048 | $1.43 \mathrm{E}-05$ |
| Area $\left(\mathrm{km}^{2}\right)$ | 2.28 | $-1.04 \mathrm{E}-02$ | 0.032 | $4.63 \mathrm{E}-04$ |
| Volume $\left(\mathrm{km}^{3}\right)$ | 0.19 | $-9.93 \mathrm{E}-04$ | 0.017 | $9.99 \mathrm{E}-03$ |
| cos (aspect) | 0.76 | $-4.60 \mathrm{E}-04$ | 0.019 | $7.06 \mathrm{E}-03$ |
| Compactness | 0.41 | $3.35 \mathrm{E}-04$ | 0.076 | $3.89 \mathrm{E}-08$ |
| Maximum elevation $(\mathrm{m})$ | 1160 | $7.00 \mathrm{E}-01$ | 0.049 | $1.29 \mathrm{E}-05$ |

Globally, the average ELA lowering was ca. 1000 m (Broecker and Denton, 1990). The less-than-average $\Delta$ ELA for Alaska has previously been attributed to a deficiency in moisture during the LGM suggesting drier-than-present conditions (e.g. Porter et al., 1983; Kaufman and Manley, 2004). Relatively gentle ELA gradients also suggest that continental climate conditions prevailed during the LGM. The major trends in the LGM ELA and glaciation thresholds for the Brooks Range, and elsewhere from Alaska, as well as the distribution of cirque-floor elevations (Péwé, 1975), show a strong component of southwesterly moisture flow across the state. In contrast, Pleistocene sand sheets distributed around central and northern Alaska show that wind directions were dominantly northeasterly (Lea and Waythomas, 1990). Evidence from loess deposits also indicates northeasterly winds during the LGM (Muhs et al., 2003). The apparent contradiction between glacial and aeolian evidence may result from differences in surface and upper atmospheric wind regimes. Episodic surface winds are responsible for moving sand and silt to form sand dunes and deposit loess, while perpetual upper-atmospheric, moisture-bearing winds affect storm tracks and control the accumulation on glaciers. Differences in the seasonal pattern of atmospheric circulation could also explain the differences in the proxy records. ELAs are mostly influenced by winter storms that carry moisture that falls as snow, as opposed to the formation of loess and dune deposits that take place during the summer when sediment is unfrozen, snow cover is absent, and barren outwash from summer ablation is abundant (Muhs et al., 2003).

## Conclusions

ELA reconstructions from the Brooks Range provide an important proxy for LGM climate trends. LGM ELAs rise from 470 m a.s.I. in the west to 1860 m a.s.I. in the eastern Brook Range. Modelled by a third-order trend surface, palaeo-ELAs lower toward the southwest across most of the range, and toward the northeast in the eastern Brooks Range. The southwestern lowering of ELAs across the range is dominant during the LGM, as it is today, indicating a source of moisture from the northern Pacific Ocean. This interpretation is similar to previous observations (e.g. Porter et al., 1983) and highlights the general stability of the regional atmospheric pressure systems, despite the impact of the Laurentide Ice Sheet on atmospheric circulation to the east (e.g. Bartlein et al., 1998). The northward lowering of LGM ELAs in the northeastern Brooks Range is probably at least in part the result of the cold temperatures where the range is farthest north and closest to the Beaufort Sea.
The residual analysis produced the somewhat unexpected result that smaller glaciers tend to lie above, rather than below,
the regional ELA trend surface. Small glaciers might be found at higher elevations because of the drying of rising air masses, or the diversion of moisture around higher elevations. This trend may be a function of an orographic influence on smaller glaciers, although this relationship may not be as strong because of the small range of glaciers sizes represented by this dataset.

LGM ELA lowering relative to modern glacier ELAs is not uniform across the Brooks Range. ELA lowering decreases toward the east from 700 to 200 m . The small amount of ELA depression in the northeastern Brooks Range has been attributed to postglacial uplift (Porter et al., 1983), but might in part be explained by the relatively low ELAs of modern glaciers that presently receive moisture from the Beaufort Sea. The average depression of LGM ELAs in the Brooks Range is similar to other mountain ranges around Alaska and less than the global average lowering. LGM aridity in this region has been attributed to increased sea-ice cover, the exposure of the Bering/Chukchi platform by eustatic sea-level lowering, colder sea-surface temperatures over the moisture source in the northern Pacific Ocean in response to lower global temperatures and increased discharge of glacier ice, and the intensification of the orographic barrier of the Alaska Range associated with the growth of the Cordilleran Ice Sheet (Porter et al., 1983). Furthermore, upper-level wind anomalies simulated for the LGM by general circulation models show a general anticyclonic curvature over Alaska, with a greater tendency for enhanced subsidence and suppression of precipitation (Bartlein et al., 1998).

Apparent contradictions in LGM atmospheric circulation patterns exist among geologic records. The opposing patterns of winds recorded from glacial and aeolian evidence are mostly the result of a difference between upper atmosphere moisture circulation and the generation of surface winds, but may also reflect seasonal differences in wind regimes.

Acknowledgements Our understanding of ELAs and their significance in reconstructing palaeoclimates has been enriched by the outstanding and inspiring research by Geoff Seltzer and his colleagues. This project was funded by National Science Foundation Grants OPP-9977972 and OPP-9977974, and a Geological Society of America graduate research grant. We thank Patrick Bartlein, Lee Dexter, Michael Ort, and two anonymous reviewers for their input, and Rob Richardson, Janelle Sikorski and Jason Briner for assistance in the field. We are also grateful to Thomas Hamilton who shared his aerial photographs and guided our recognition of LGM moraines in the Brooks Range.

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Appendix: Physical characteristics for all reconstructed last glacial maximum valley glaciers

| Region | UTM Albers Easting ${ }^{\text {a }}$ | UTM Albers Northing ${ }^{\text {a }}$ | Lowest elevation (m) | Highest elevation (m) | Average elevation (m) | Elevation range (m) | Area ( $\mathrm{km}^{2}$ ) | Perimeter (km) | Compactness | Aspect <br> ( ${ }^{\circ}$ | Slope <br> $\left({ }^{\circ}\right)$ | Length (km) | Width (km) | Volume ( $\mathrm{km}^{3}$ ) | $\begin{aligned} & \text { ELA } \\ & (\mathrm{m}) \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Eastern Brooks Range | 336304 | 2192999 | 817 | 1546 | 1248 | 729 | 3.02 | 14.4 | 0.18 | 4 | 9 | 1.9 | 1.59 | 0.26 | 1306 |
|  | 341427 | 2185443 | 772 | 1494 | 1102 | 722 | 1.68 | 9.0 | 0.26 | 350 | 15 | 2.2 | 0.76 | 0.12 | 1037 |
|  | 340459 | 2185342 | 902 | 1471 | 1133 | 569 | 0.49 | 4.6 | 0.29 | 328 | 17 | 1.1 | 0.44 | 0.01 | 1067 |
|  | 338619 | 2184197 | 1026 | 1352 | 1225 | 326 | 0.27 | 2.5 | 0.54 | 14 | 20 | 0.7 | 0.39 | 0.01 | 1235 |
|  | 401688 | 2183485 | 1163 | 2265 | 1810 | 1102 | 6.71 | 24.4 | 0.14 | 337 | 11 | 5.4 | 1.24 | 0.52 | 1709 |
|  | 466340 | 2190943 | 924 | 1447 | 1180 | 523 | 0.73 | 4.4 | 0.47 | 6 | 16 | 1.5 | 0.49 | 0.05 | 1155 |
|  | 468224 | 2190420 | 1012 | 1621 | 1379 | 609 | 1.16 | 5.5 | 0.48 | 7 | 16 | 1.7 | 0.68 | 0.12 | 1374 |
|  | 474787 | 2188885 | 1318 | 1666 | 1538 | 348 | 0.46 | 3.4 | 0.52 | 352 | 17 | 0.9 | 0.52 | 0.03 | 1555 |
|  | 471575 | 2184869 | 1139 | 1845 | 1556 | 706 | 2.10 | 9.5 | 0.29 | 337 | 12 | 2.2 | 0.95 | 0.12 | 1515 |
|  | 466645 | 2184069 | 1219 | 1825 | 1540 | 606 | 1.50 | 8.4 | 0.27 | 17 | 11 | 1.9 | 0.79 | 0.10 | 1501 |
|  | 470230 | 2184256 | 1272 | 1857 | 1661 | 585 | 1.90 | 7.2 | 0.46 | 320 | 12 | 2.3 | 0.83 | 0.21 | 1674 |
|  | 477233 | 2185086 | 1153 | 1637 | 1412 | 484 | 1.45 | 5.6 | 0.57 | 16 | 13 | 1.5 | 0.96 | 0.06 | 1398 |
|  | 468485 | 2183364 | 1240 | 1857 | 1604 | 617 | 2.12 | 10.1 | 0.26 | 337 | 12 | 2.1 | 1.01 | 0.16 | 1598 |
|  | 472891 | 2184526 | 1559 | 1928 | 1788 | 369 | 0.57 | 3.6 | 0.55 | 345 | 13 | 1.1 | 0.51 | 0.04 | 1787 |
|  | 478891 | 2184362 | 1142 | 1671 | 1483 | 529 | 1.02 | 4.7 | 0.58 | 15 | 15 | 1.3 | 0.78 | 0.10 | 1492 |
|  | 456176 | 2179967 | 704 | 2066 | 1365 | 1362 | 12.39 | 44.5 | 0.08 | 324 | 9 | 5.3 | 2.34 | 0.92 | 1288 |
|  | 480080 | 2184066 | 1169 | 1702 | 1504 | 533 | 0.97 | 4.6 | 0.59 | 3 | 15 | 1.4 | 0.69 | 0.09 | 1515 |
|  | 448433 | 2179831 | 1127 | 1690 | 1456 | 563 | 2.07 | 8.0 | 0.40 | 21 | 10 | 2.2 | 0.94 | 0.17 | 1438 |
|  | 460924 | 2179498 | 836 | 1990 | 1568 | 1154 | 6.83 | 22.3 | 0.17 | 3 | 10 | 4.6 | 1.49 | 0.80 | 1555 |
|  | 493270 | 2180877 | 596 | 2114 | 1657 | 1518 | 7.51 | 20.9 | 0.22 | 13 | 10 | 6.1 | 1.23 | 1.45 | 1676 |
|  | 490959 | 2181418 | 822 | 1859 | 1543 | 1037 | 3.49 | 12.7 | 0.27 | 14 | 10 | 3.5 | 1.00 | 0.47 | 1578 |
|  | 488661 | 2183090 | 1027 | 1268 | 1177 | 241 | 0.38 | 3.5 | 0.40 | 7 | 9 | 0.9 | 0.42 | 0.01 | 1179 |
|  | 468410 | 2179129 | 927 | 2060 | 1539 | 1133 | 9.62 | 35.3 | 0.10 | 333 | 9 | 3.7 | 2.60 | 0.96 | 1475 |
|  | 445551 | 2175607 | 973 | 2017 | 1645 | 1044 | 7.15 | 21.2 | 0.20 | 347 | 10 | 5.3 | 1.35 | 0.87 | 1651 |
|  | 476128 | 2178246 | 667 | 1812 | 1398 | 1145 | 5.93 | 23.4 | 0.14 | 349 | 10 | 4.8 | 1.24 | 0.57 | 1397 |
|  | 463280 | 2177892 | 958 | 2040 | 1620 | 1082 | 4.77 | 15.4 | 0.25 | 17 | 11 | 4.9 | 0.97 | 0.56 | 1540 |
|  | 448343 | 2177023 | 1232 | 1972 | 1677 | 740 | 2.19 | 10.4 | 0.25 | 43 | 14 | 2.5 | 0.88 | 0.15 | 1687 |
|  | 478048 | 2177965 | 609 | 1717 | 1392 | 1108 | 3.11 | 12.7 | 0.24 | 22 | 10 | 3.9 | 0.80 | 0.25 | 1411 |
|  | 471154 | 2177919 | 1059 | 1863 | 1599 | 804 | 3.91 | 11.8 | 0.36 | 35 | 11 | 3.0 | 1.30 | 0.34 | 1578 |
|  | 438252 | 2174681 | 1452 | 1854 | 1691 | 402 | 0.48 | 3.2 | 0.57 | 311 | 20 | 0.8 | 0.59 | 0.03 | 1692 |
|  | 472328 | 2177146 | 1210 | 1832 | 1626 | 622 | 1.01 | 6.4 | 0.31 | 50 | 13 | 2.1 | 0.48 | 0.05 | 1635 |
|  | 479288 | 2177138 | 1320 | 1789 | 1608 | 469 | 0.79 | 4.9 | 0.41 | 6 | 14 | 1.4 | 0.56 | 0.03 | 1605 |
|  | 494586 | 2178629 | 1474 | 2037 | 1803 | 563 | 1.31 | 5.5 | 0.54 | 353 | 15 | 1.6 | 0.82 | 0.11 | 1790 |
|  | 496169 | 2178670 | 1514 | 1845 | 1721 | 331 | 0.60 | 4.1 | 0.46 | 24 | 10 | 1.1 | 0.55 | 0.03 | 1724 |
|  | 495286 | 2176437 | 1592 | 1994 | 1809 | 402 | 0.83 | 4.3 | 0.56 | 21 | 17 | 1.1 | 0.75 | 0.03 | 1804 |
|  | 444189 | 2170227 | 1212 | 1854 | 1533 | 642 | 1.55 | 7.6 | 0.34 | 304 | 12 | 2.2 | 0.70 | 0.11 | 1465 |
|  | 427931 | 2167906 | 1225 | 2139 | 1754 | 914 | 1.79 | 8.9 | 0.29 | 39 | 13 | 2.0 | 0.89 | 0.14 | 1733 |
|  | 433206 | 2155399 | 1416 | 1918 | 1690 | 502 | 1.13 | 6.7 | 0.31 | 344 | 12 | 1.5 | 0.75 | 0.06 | 1654 |
|  | 426346 | 2153801 | 1363 | 1946 | 1661 | 583 | 0.97 | 6.8 | 0.26 | 17 | 12 | 1.9 | 0.51 | 0.03 | 1636 |
|  | 432528 | 2154852 | 1575 | 1977 | 1814 | 402 | 0.67 | 3.8 | 0.57 | 353 | 13 | 1.2 | 0.56 | 0.05 | 1819 |
|  | 427093 | 2153043 | 1531 | 2005 | 1806 | 474 | 0.63 | 4.3 | 0.43 | 5 | 16 | 1.2 | 0.53 | 0.04 | 1795 |
|  | 427890 | 2153006 | 1498 | 2009 | 1805 | 511 | 0.84 | 4.7 | 0.48 | 29 | 16 | 1.3 | 0.65 | 0.05 | 1799 |
|  | 431618 | 2153567 | 1647 | 2000 | 1855 | 353 | 0.43 | 3.1 | 0.55 | 346 | 16 | 0.9 | 0.48 | 0.02 | 1859 |
|  | 428572 | 2152897 | 1480 | 1805 | 1681 | 325 | 0.33 | 3.0 | 0.47 | 36 | 15 | 1.0 | 0.33 | 0.01 | 1696 |

















Appendix: Continued







 No







| Region | UTM Albers Easting ${ }^{\text {a }}$ | UTM Albers Northing ${ }^{\text {a }}$ | Lowest elevation (m) | Highest elevation (m) | Average elevation (m) | Elevation range (m) | $\begin{aligned} & \text { Area } \\ & \left(\mathrm{km}^{2}\right) \end{aligned}$ | Perimeter (km) | Compactness | Aspect <br> $\left(^{\circ}\right)$ | Slope $\left({ }^{\circ}\right)$ | Length (km) | Width (km) | Volume $\left(\mathrm{km}^{3}\right)$ | $\begin{aligned} & \text { ELA } \\ & (\mathrm{m}) \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | Region




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Appendix：Continued

| Region | UTM Albers Easting ${ }^{\text {a }}$ | UTM Albers Northing ${ }^{\text {a }}$ | Lowest elevation（m） | Highest elevation（m） | Average elevation（m） | Elevation range（m） | $\begin{aligned} & \text { Area } \\ & \left(\mathrm{km}^{2}\right) \end{aligned}$ | Perimeter （km） | Compactness | Aspect <br> $\left({ }^{\circ}\right)$ | Slope $\left({ }^{\circ}\right)$ | Length （km） | Width （km） | Volume $\left(\mathrm{km}^{3}\right)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |

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Appendix: Continued

| Region | UTM Albers Easting ${ }^{\text {a }}$ | UTM Albers Northing ${ }^{\text {a }}$ | Lowest elevation (m) | Highest elevation (m) | Average elevation (m) | Elevation range (m) | Area ( $\mathrm{km}^{2}$ ) | Perimeter (km) | Compactness | Aspect <br> $\left({ }^{\circ}\right)$ | Slope <br> $\left(^{\circ}\right)$ | Length (km) | Width (km) | Volume ( $\mathrm{km}^{3}$ ) | $\begin{aligned} & \text { ELA } \\ & (\mathrm{m}) \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Western Brooks Range | -257751 | 2081572 | 1148 | 1376 | 1280 | 228 | 0.29 | 2.6 | 0.53 | 17 | 16 | 0.6 | 0.49 | 0.01 | 1278 |
|  | -258927 | 2078800 | 913 | 1134 | 1052 | 221 | 0.22 | 2.0 | 0.67 | 39 | 17 | 0.5 | 0.45 | 0.01 | 1059 |
|  | -340691 | 2073305 | 449 | 774 | 623 | 325 | 0.61 | 4.8 | 0.33 | 331 | 10 | 1.6 | 0.38 | 0.02 | 614 |
|  | -343227 | 2072655 | 462 | 857 | 646 | 395 | 2.80 | 16.4 | 0.13 | 353 | 8 | 3.0 | 0.93 | 0.10 | 606 |
|  | -279575 | 2068233 | 879 | 1084 | 984 | 205 | 0.21 | 2.2 | 0.57 | 354 | 19 | 0.5 | 0.42 | 0.01 | 997 |
|  | -280347 | 2067634 | 812 | 1046 | 959 | 234 | 0.55 | 4.0 | 0.44 | 13 | 11 | 1.1 | 0.50 | 0.03 | 969 |
|  | -281897 | 2066377 | 686 | 1077 | 884 | 391 | 0.56 | 4.0 | 0.45 | 317 | 16 | 1.1 | 0.51 | 0.03 | 855 |
|  | -348990 | 2070152 | 438 | 872 | 591 | 434 | 3.67 | 19.3 | 0.12 | 35 | 6 | 3.8 | 0.97 | 0.13 | 549 |
|  | -275574 | 2060604 | 467 | 1254 | 807 | 787 | 8.52 | 33.6 | 0.09 | 317 | 7 | 5.3 | 1.61 | 0.53 | 797 |
|  | $-351921$ | $2067325$ | 515 | 845 | 714 | 330 | 0.88 | 5.5 | 0.36 | 316 | 10 | 1.7 | 0.52 | 0.04 | 712 |
|  | $-270658$ | $2060538$ | 590 | 1205 | 873 | 615 | 4.78 | 16.3 | 0.23 | 6 | 8 | 2.9 | 1.65 | 0.31 | 828 |
|  | -353933 | 2066338 | 441 | 819 | 620 | 378 | 0.85 | 5.8 | 0.32 | 324 | 11 | 1.6 | 0.53 | 0.03 | 605 |
|  | -185697 | 2051066 | 578 | 1204 | 793 | 626 | 9.07 | 25.8 | 0.17 | 343 | 4 | 3.8 | 2.39 | 0.34 | 717 |
|  | -269493 | 2059021 | 640 | 1066 | 879 | 426 | 1.85 | 10.8 | 0.20 | 42 | 8 | 1.6 | 1.15 | 0.03 | 837 |
|  | -273559 | 2057414 | 638 | 1115 | 903 | 477 | 6.09 | 21.7 | 0.16 | 88 | 6 | 3.3 | 1.85 | 0.42 | 887 |
|  | -277150 | 2057322 | 622 | 1157 | 923 | 535 | 5.57 | 17.2 | 0.24 | 294 | 7 | 2.8 | 1.99 | 0.48 | 891 |
|  | -355793 | 2063193 | 564 | 837 | 734 | 273 | 0.87 | 5.8 | 0.33 | 332 | 7 | 1.6 | 0.54 | 0.05 | 747 |
|  | -325914 | 2060725 | 643 | 1017 | 828 | 374 | 0.71 | 4.0 | 0.57 | 356 | 13 | 1.1 | 0.64 | 0.06 | 826 |
|  | $-178185$ | $2049183$ | 542 | 1019 | 797 | 477 | 4.10 | 13.6 | 0.28 | 135 | 5 | 3.5 | 1.17 | 0.28 | 789 |
|  | $-181574$ | $2047771$ | 491 | 1102 | 749 | 611 | 10.26 | 30.0 | 0.14 | 144 | 5 | 6.3 | 1.63 | 0.60 | 742 |
|  | -189833 | 2049412 | 894 | 1063 | 985 | 169 | 0.39 | 3.0 | 0.55 | 340 | 9 | 0.8 | 0.49 | 0.01 | 988 |
|  | -188081 | 2049279 | 887 | 1051 | 983 | 164 | 0.25 | 2.3 | 0.60 | 354 | 11 | 0.6 | 0.41 | 0.00 | 985 |
|  | -273376 | 2052451 | 527 | 1161 | 808 | 634 | 11.88 | 26.3 | 0.22 | 110 | 4 | 5.7 | 2.08 | 1.07 | 745 |
|  | -280391 | 2052016 | 510 | 1223 | 809 | 713 | 10.91 | 29.0 | 0.16 | 243 | 5 | 5.9 | 1.85 | 0.86 | 729 |
|  | -326927 | 2056744 | 751 | 1092 | 894 | 341 | 0.67 | 3.8 | 0.57 | 326 | 15 | 1.0 | 0.67 | 0.05 | 875 |
|  | $-327906$ | 2056637 | 609 | 1035 | 829 | 426 | 0.84 | 4.7 | 0.48 | 327 | 12 | 1.5 | 0.56 | 0.04 | 817 |
|  | $-325670$ | $2055639$ | 635 | 952 | 794 | 317 | 1.75 | 7.6 | 0.38 | 109 | 10 | 1.6 | 1.09 | 0.10 | 799 |
|  | $-294891$ | $2049686$ | 319 | 928 | 637 | 609 | 2.75 | 14.6 | 0.16 | 306 | 9 | 3.0 | 0.92 | 0.12 | 611 |
|  | $-319993$ | $2051825$ | 601 | 906 | 779 | 305 | 0.67 | 3.6 | 0.65 | 31 | 14 | 1.0 | 0.67 | 0.03 | 779 |
|  | $-292997$ | $2049009$ | 839 | 1089 | 991 | 250 | 0.49 | 3.2 | 0.58 | 17 | 15 | 0.8 | 0.61 | 0.02 | 996 |
|  | -332276 | 2051528 | 674 | 960 | 813 | 286 | 0.37 | 3.8 | 0.31 | 331 | 13 | 1.1 | 0.33 | 0.01 | 814 |
|  | -329609 | 2050618 | 483 | 946 | 653 | 463 | 2.70 | 11.4 | 0.26 | 359 | 9 | 3.1 | 0.87 | 0.10 | 604 |
|  | -291293 | 2047393 | 456 | 929 | 661 | 473 | 6.57 | 21.0 | 0.19 | 67 | 4 | 3.8 | 1.73 | 0.31 | 637 |
|  | -335344 | 2050201 | 641 | 849 | 750 | 208 | 0.46 | 3.5 | 0.48 | 287 | 12 | 1.0 | 0.46 | 0.02 | 751 |
|  | $-336271$ | $2049970$ | 760 | 958 | 840 | 198 | 0.33 | 3.1 | 0.42 | 289 | 12 | 0.9 | 0.36 | 0.01 | 822 |
|  | $-328490$ | $2049284$ | 483 | 877 | 681 | 394 | 1.13 | 5.9 | 0.41 | 33 | 12 | 1.9 | 0.59 | 0.06 | 663 |
|  | $-331599$ | $2049093$ | 607 | 924 | 743 | 317 | 0.53 | 4.2 | 0.38 | 311 | 18 | 1.0 | 0.53 | 0.01 | 730 |
|  | $-334398$ | 2048999 | 520 | 788 | 651 | 268 | 1.30 | 6.2 | 0.42 | 85 | 6 | 1.9 | 0.69 | 0.06 | 622 |
|  | -295356 | 2045783 | 732 | 1094 | 903 | 362 | 0.98 | 5.4 | 0.42 | 300 | 10 | 1.6 | 0.61 | 0.04 | 886 |
|  | -328381 | 2048262 | 529 | 798 | 670 | 269 | 0.37 | 4.0 | 0.29 | 50 | 10 | 0.8 | 0.46 | 0.01 | 666 |
|  | -328776 | 2046979 | 746 | 901 | 817 | 155 | 0.14 | 1.8 | 0.56 | 16 | 16 | 0.5 | 0.29 | 0.00 | 819 |
|  | -268675 | 2040351 | 457 | 893 | 652 | 436 | 5.65 | 18.2 | 0.21 | 26 | 5 | 4.5 | 1.26 | 0.32 | 584 |
|  | -271988 | 2039881 | 658 | 900 | 790 | 242 | 0.45 | 3.2 | 0.54 | 337 | 14 | 0.8 | 0.57 | 0.02 | 790 |
|  | $-274805$ | $2039553$ | $573$ | $734$ | 670 | 161 | 0.25 | 2.3 | 0.60 | 333 | 12 | 0.5 | 0.50 | 0.01 | 675 |
|  | -229272 | 1981929 | 929 | 1190 | 1111 | 261 | 0.46 | 3.4 | 0.52 | 12 | 11 | 0.9 | 0.52 | 0.04 | 1129 |














 | -230723 | 1981979 |
| :--- | :--- |
| -232003 | 1981895 |
| -228232 | 1981254 |
| -229719 | 1980827 |
| -310356 | 1984365 |
| -306581 | 1983789 |
| -310097 | 1982911 |
| -314324 | 1976406 |
| -310176 | 1975982 |
| -302421 | 1975173 |
| -309194 | 1975312 |
| -310942 | 1974604 |
| -317396 | 1974121 |
| -211498 | 1966062 |
| -310279 | 1972044 |
| -203652 | 1963256 |
| -304647 | 1970374 |
| -213875 | 1960261 |
| -205715 | 1959226 |
| -204169 | 1958032 |
| -187464 | 1954672 |
| -201566 | 1955622 |
| -212063 | 1956176 |
| -186532 | 1954182 |
| -183732 | 1952773 |
| -188958 | 1953349 |
| -200057 | 1953952 |
| -182170 | 1951816 |
| -158000 | 1950270 |
| -180594 | 1951038 |
| -179468 | 1950713 |
| -190377 | 1951423 |
| -212018 | 1952762 |
| -178985 | 1949899 |
| -198806 | 1951285 |
| -225077 | 1952251 |
| -176469 | 1948750 |
| -207576 | 1950632 |
| -209014 | 1949245 |
| -192080 | 1948142 |
| -165708 | 1946133 |
| -209888 | 1948892 |
| -168695 | 1945883 |
| -166509 | 1945955 |
| -167370 | 1945781 |
| -207595 | 1948779 |
| -226418 | 1949719 |
| -220956 | 1949069 |

Appendix: Continued

| Region | UTM Albers Easting ${ }^{\text {a }}$ | UTM Albers Northing ${ }^{\text {a }}$ | Lowest elevation (m) | Highest elevation (m) | Average elevation (m) | Elevation range (m) | Area ( $\mathrm{km}^{2}$ ) | Perimeter (km) | Compactness | Aspect <br> $\left({ }^{\circ}\right)$ | Slope <br> $\left(^{\circ}\right)$ | Length (km) | Width (km) | Volume $\left(\mathrm{km}^{3}\right)$ | $\begin{aligned} & \text { ELA } \\ & (\mathrm{m}) \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | -176757 | 1945780 | 470 | 787 | 628 | 317 | 0.58 | 3.7 | 0.53 | 13 | 17 | 1.0 | 0.58 | 0.04 | 620 |
|  | -206824 | 1947763 | 433 | 717 | 545 | 284 | 0.54 | 4.0 | 0.43 | 9 | 14 | 1.1 | 0.49 | 0.02 | 529 |
|  | -164812 | 1944389 | 567 | 729 | 637 | 162 | 0.44 | 3.1 | 0.56 | 19 | 9 | 0.8 | 0.54 | 0.01 | 635 |
|  | -171790 | 1943426 | 424 | 666 | 549 | 242 | 0.69 | 4.0 | 0.55 | 5 | 9 | 1.1 | 0.63 | 0.04 | 542 |
|  | -266627 | 1946384 | 543 | 772 | 660 | 229 | 0.48 | 3.1 | 0.62 | 357 | 13 | 0.8 | 0.60 | 0.01 | 663 |
|  | -268086 | 1945475 | 708 | 1010 | 847 | 302 | 0.88 | 4.7 | 0.50 | 339 | 12 | 1.3 | 0.68 | 0.02 | 821 |
|  | -175072 | 1926677 | 536 | 703 | 603 | 167 | 0.86 | 4.4 | 0.55 | 8 | 7 | 1.1 | 0.78 | 0.04 | 594 |
|  | -176867 | 1926156 | 424 | 601 | 517 | 177 | 0.65 | 4.3 | 0.44 | 322 | 10 | 1.0 | 0.65 | 0.02 | 517 |
|  | -268827 | 1932183 | 431 | 723 | 606 | 292 | 1.62 | 6.5 | 0.48 | 14 | 7 | 1.9 | 0.85 | 0.09 | 605 |
|  | -180199 | 1926110 | 511 | 707 | 607 | 196 | 0.26 | 2.3 | 0.62 | 28 | 18 | 0.5 | 0.51 | 0.01 | 609 |
|  | -173057 | 1925326 | 516 | 665 | 587 | 149 | 0.22 | 2.3 | 0.52 | 12 | 11 | 0.6 | 0.36 | 0.01 | 586 |
|  | -177963 | 1925281 | 533 | 703 | 614 | 170 | 0.38 | 2.8 | 0.62 | 334 | 13 | 0.7 | 0.54 | 0.02 | 613 |
|  | -172482 | 1924923 | 537 | 659 | 591 | 122 | 0.21 | 2.0 | 0.63 | 16 | 12 | 0.5 | 0.42 | 0.00 | 589 |
|  | -171166 | 1923146 | 496 | 638 | 553 | 142 | 0.17 | 1.9 | 0.59 | 346 | 12 | 0.5 | 0.35 | 0.01 | 550 |
|  | -170152 | 1922949 | 503 | 687 | 587 | 184 | 0.49 | 3.2 | 0.59 | 13 | 11 | 0.8 | 0.62 | 0.03 | 573 |


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